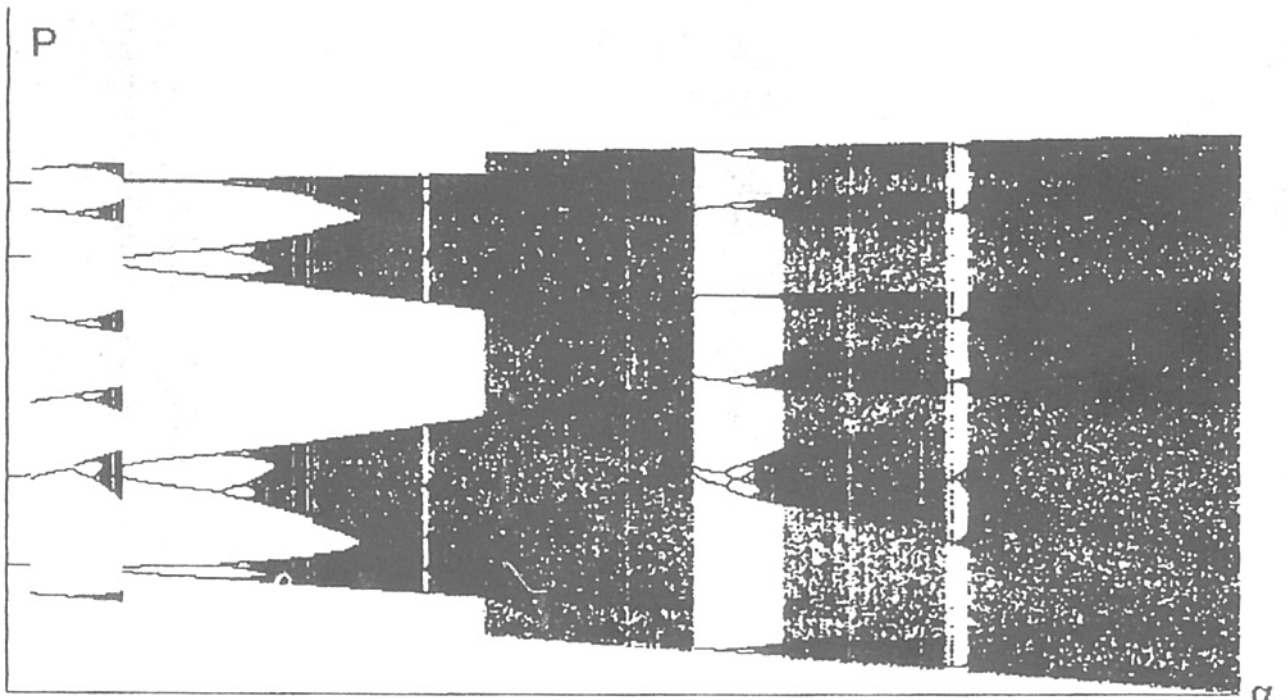


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# Geometrical Model of Anticipatory Embedded Systems

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## Abstract

I have defined (Garnier-Malet, 1997) the fundamental movement of doubling which transforms any initial system into anticipatory (Rosen, 1985) embedded (Dubois, 1996 and 1997) systems. I have demonstrated that six levels of embedding are necessary in the initial system which is the zero level during its transformation. Each level has its observer. With scalings of transformation's spaces and times, each level is a zero level. During the doubling transformation the initial observer cannot observe the other observers. But, at the end of the transformation which is always the beginning of another transformation, the initial and the third observers, then the third and the sixth observers, exchange their space's and time's perception.

These exchanges are the only way for the initial observer to know and anticipate the consequences of an experience of embedded systems before having time to realise it in the initial system and, above all, without modifying this initial space. The perception's exchange of the observers must be the consequences of this necessity at the end of the transformation. These exchanges imply three speeds of doubling which I have calculated. They are necessary at the end to juxtapose the six embedded levels in the initial system which must be necessarily one ten-dimensional space. We shall see that this implication is as fundamental as the movement of doubling.

**Keywords** : observers, perception, anticipation, scaling, dilation or expansion of spaces.

## 1. Introduction

An application to the solar system (Garnier-Malet, 1997) which is anticipatory embedded systems (I have found the mathematical link between six double planetary levels) has allowed me to calculate the speed of the doubling transformation. For the human observers who are in the third solar level, this constant speed is the speed of light  $C=299\ 792\ \text{km./s}$ .

In this application, I have demonstrated that 24 840 years are the time of one cycle of the solar doubling transformation. Now, we are almost at the end of this doubling time. Only at this end, the third solar observers (who we are) can observe the space and time of the initial or the sixth observer. With the speed of light, two other speeds of doubling transformation give to the third observer three perceptions of the surrounding spaces when all the levels are juxtaposed.

Before explaining this three perceptions and their consequences in our Universe, I am going to remind you the fundamental movement of doubling.

## 2. The Fundamental Movement of Doubling

With scalings of spaces and times, the movement of doubling allows each level to make the same transformation but not in the same time. This movement is fundamental because it can be applied to a particle and to a space. This double application is the condition of observers' exchanges. In fact, a perceivable space of an embedded observer  $o_n$  is always a perceivable particle of an initial observer  $o_0$ . The value of  $n$  determines a limit of perception of a space for  $o_n$  and a limit of perception of a particle for  $o_0$ .

The initial observer  $o_0$  is at the centre of a spherical space  $\alpha_0$  (radius  $R_0=2^n R_n$ ). The surface of  $\alpha_0$  is the horizon of  $o_0$ . For  $o_0$ , the smallest perceivable particle on  $\alpha_0$  is a spherical space  $\alpha_n$  (radius  $R_n$ ). The initial movement of  $\alpha_n$  on  $\alpha_0$  is observed by  $o_0$  in a plane  $P_0(x_0, y_0)$  which determines a circular horizon  $2\pi R_0=\Omega_0$  on the sphere  $\alpha_0$  (fig. 1).  $P_0$  is a privileged plane for  $o_0$  which observes the initial movement of  $\alpha_n$  in  $\alpha_0$ .

Afterwards, I always characterise the spherical space  $\alpha_n$  of  $o_n$  by the horizon  $\Omega_n, \forall n$ .

With scalings of spaces and times,  $o_n$  is ( $\forall n$ ) the initial observer of the particle  $\Omega_{2n}$  in the space  $\Omega_n$ .

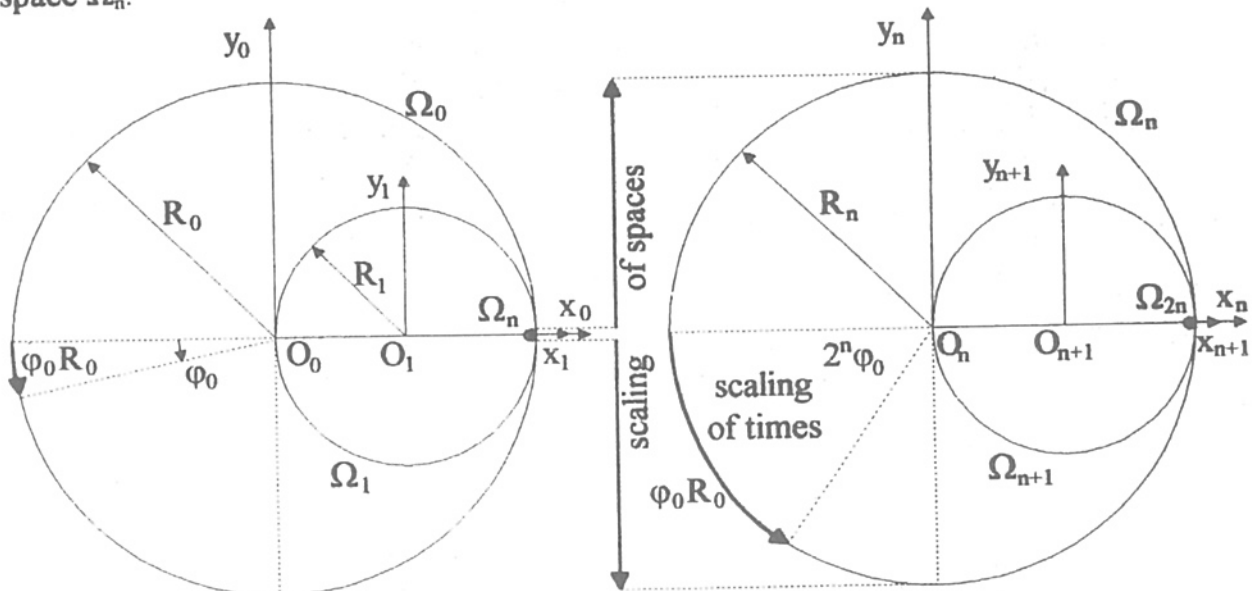


Figure 1 : scalings of spaces and times between  $o_0$  and  $o_n$ .

### 2.1. Fusion and Fission of the Particle by Spinback

Initially,  $P_0, P_1, \dots, P_n$  are juxtaposed.  $\Omega_0, \Omega_1, \dots, \Omega_n$  are tangential in the same point. For  $o_0$ , this point is the perceivable particle  $\Omega_n$  inside  $\Omega_0$ . For  $o_n$ ,  $\Omega_0, \Omega_1, \dots, \Omega_n$  are tangential in the point  $\Omega_{2n}$  which is the smallest perceivable particle for  $o_n$ .

At the centre of  $\Omega_0$ ,  $o_0$  observes the rotation  $\varphi_0$  of  $2\Omega_n$  on  $\Omega_0$  (fig. 2). The speed of this rotation is constant.

$\forall n$ , at the centre of  $\Omega_n$ ,  $o_n$  observes the rotation  $\varphi_n = \varphi_0 / 2^n$  of  $2\Omega_{2n}$  on  $\Omega_n$ .

During this rotation  $\varphi_0$  of the radius  $R_0$  (corresponding to  $2\Omega_n$ ), the plane  $P_1(x_1, y_1)$  makes a rotation  $\varphi_0$  around this radius. The rotation  $\pi$  of  $2\Omega_n$  on  $\Omega_0$  turns back  $P_1$  in  $P_0$  and reverses the movement of  $\Omega_1$  in  $\Omega_0$ . I have called this movement the spinback of the space  $\Omega_1$  into  $\Omega_0$ . The spinback of  $\Omega_1$  is a movement of fission and fusion of the particles  $\Omega_n, \Omega_{n+1}, \dots, \Omega_{2n}$ . It doesn't remake the initial state.

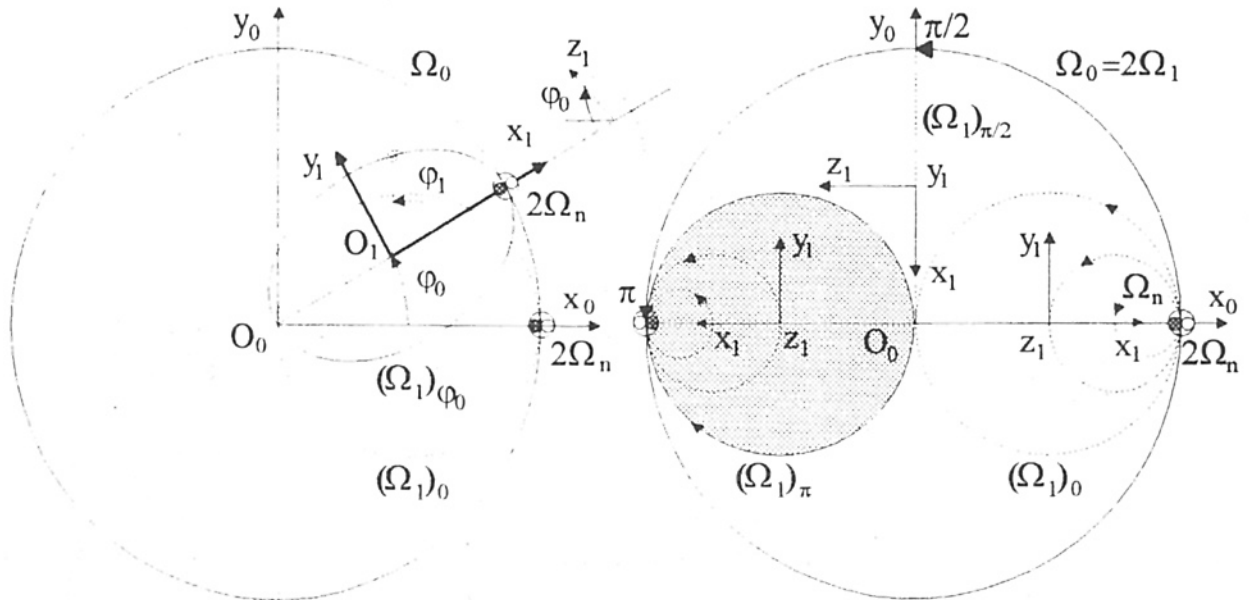


Figure 2 : the spinback.

The particles  $\Omega_{n+1}, \Omega_{n+2}, \dots, \Omega_{2n}$  have reversed their position into  $\Omega_n$  which has reversed its movement into  $P_0$ . This movement which modifies the properties of the particle without modifying its envelope, can explain the spin of the particles and the spin of the spaces (that is to say the gravitation).

By definition, the spinback in the space  $\Omega_n$  is  $2^n$  faster than the spinback in the space  $\Omega_0$ . So,  $o_n$  can observe  $2^n$  times the transformation which is observed only once by  $o_0$ .

## 2.2. Negative Time and Imaginary Dilated Space

The initial observer can imagine a virtual observer  $o_{.1}$  in a virtual space  $\Omega_{.1}$  (fig. 3) where the time of one spinback of  $\Omega_{.1}$  is the time of two spinbacks of  $\Omega_0$ .

This observer  $o_{.1}$  can perceive the outside of  $\Omega_0$  in  $2\Omega_0$  and the particle  $2\Omega_n$  but not the particle  $\Omega_n$ . For  $o_{.1}$ , the time of the no perceivable spinback of  $\Omega_n$  into  $2\Omega_n$  is the time of the rotation  $\pi$  of  $2\Omega_n$  on  $\Omega_0$ . For  $o_{.1}$ , it is a negative time of a virtual rotation  $\varphi_{.1} = \varphi_0/2 = \pi/2$  of  $\Omega_0$  in this virtual space.

For  $o_0$ , this virtual initial dilated space  $\Omega_{.1} = 2\Omega_0$  seems to be the consequence of a virtual path of  $\Omega_0$  in this space, during the rotation  $\varphi_{.1} = \pi/2$  which transforms (in a negative time) a negative imaginary space  $-i\Omega_{.1}$  into a real space  $(i) \times -i\Omega_{.1} = \Omega_{.1}$ .

The complex number  $i$  (with  $i^2=-1$ ) can be the operator of this rotation and this dilation. It corresponds to the rotation  $\pi/2$  of the particle ( $R_0 e^{i\varphi_0}$ ) in the plane and to the rotation  $\pi/2$  of the plane of  $\Omega_0$  in the space. It is logical because, by definition, the horizon  $\Omega_0$  of the initial observer is also the horizon of a particle for another observer. For  $o_0$ , the virtual observer  $o_{-1}$  is at the centre of the particle  $2\Omega_n$ .

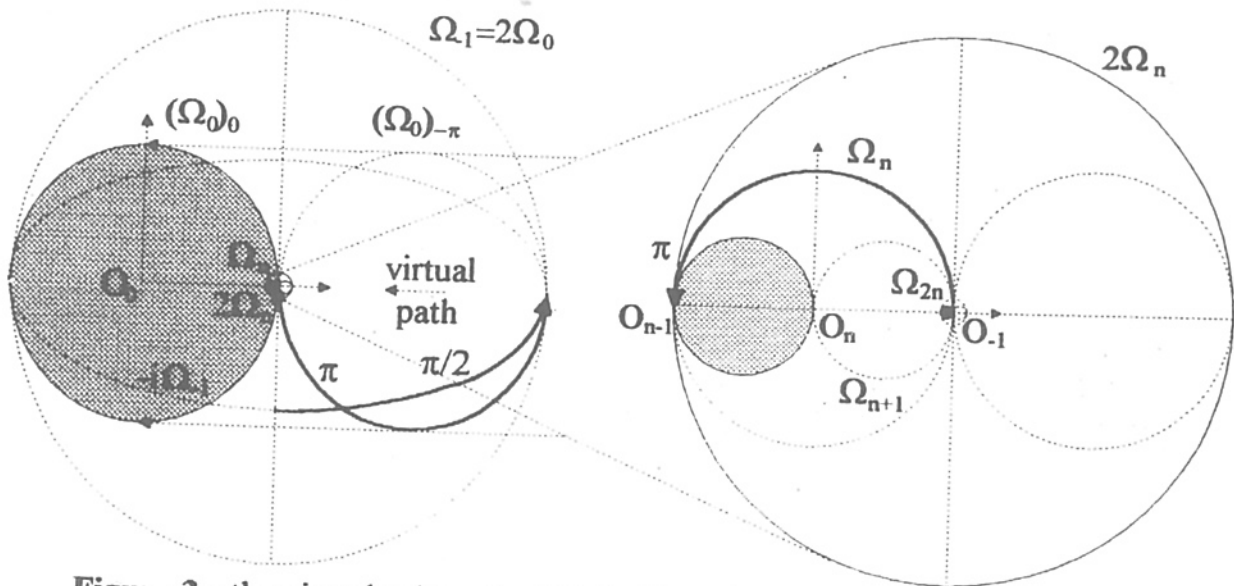


Figure 3 : the virtual spinback of  $\Omega_0$  in  $\Omega_1$  and the real spinback in  $\Omega_{n+1}$  in  $\Omega_n$ .

The spinback of  $\Omega_{n+1}$  in  $\Omega_n$  (no perceivable by  $o_0$ ) is faster ( $\times 2^n$ ) than the spinback of  $\Omega_1$  in  $\Omega_0$ . It allows  $o_{-1}$  and  $o_n$  to exchange their place twice. If the particle  $\Omega_n$  can dilate its space and can become  $2^n \Omega_n$  during the spinback of  $2\Omega_n$  on  $\Omega_0$ ,  $\Omega_0$  and  $2^n \Omega_n = \Omega_0$  can be juxtaposed. So,  $o_0$  and  $o_n$  can exchange their place :  $o_0$  becomes  $o_n$  when  $o_n$  becomes  $o_{-1}$ . Then,  $o_n$  becomes  $o_0$  again when  $o_{-1}$  becomes  $o_n$ . These exchanges which can continue between  $o_n$  and  $o_{2n}$  use two kinds of particles' paths. The observers' exchanges are also paths' exchanges during the juxtaposition of  $\Omega_0$  and the dilated space  $\Omega_n$ .

### 2.3. Tangential and Radial Paths

For  $o_0$ , the spinback of  $2\Omega_n$  on  $\Omega_0$  is a tangential path on the space  $\Omega_0$  (fig. 4).

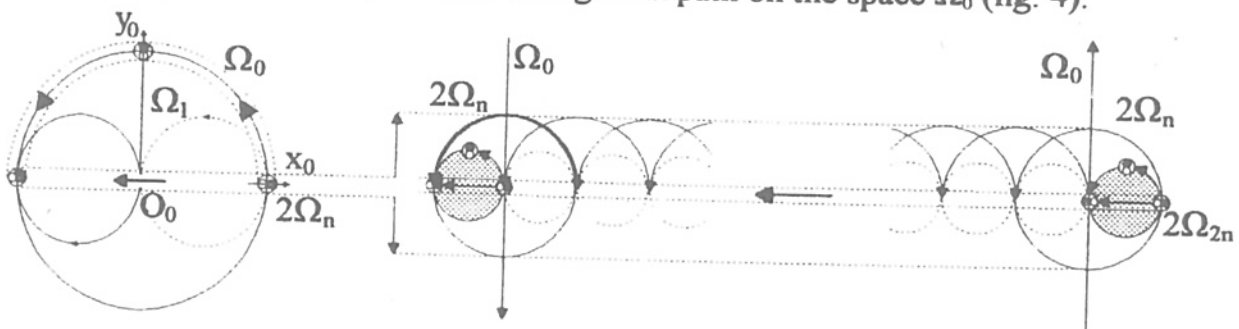
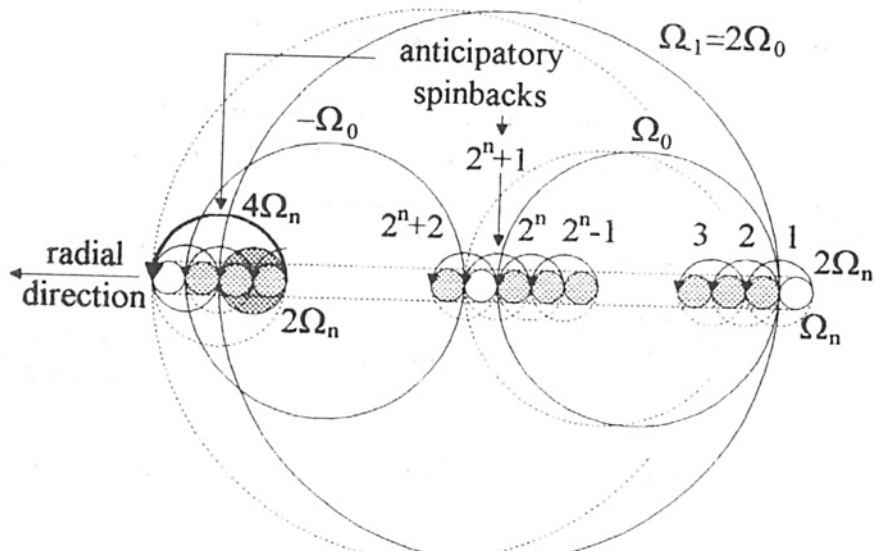


Figure 4 : radial and tangential embedded paths of  $2\Omega_n$ .

For  $o_0$ ,  $2^n$  radial spinbacks of  $\Omega_n$  into  $2\Omega_n$  seems to be a radial path into  $\Omega_0$ . So, there are two kinds of spaces' or particles' paths : radial or tangential.  
 For  $o_0$ , the tangential path of  $2\Omega_n$  on  $\Omega_0$  is  $\pi R_0$ . The radial path of  $2\Omega_n$  into  $\Omega_0$  which corresponds to  $2^n$  spinbacks of  $\Omega_n$  into  $2\Omega_n$ , is also  $\pi R_0$  (by definition :  $2^n \pi R_n = 2^n \pi R_0 / 2^n$ ).  
 So, during the spinback of  $\Omega_1$  in  $\Omega_0$ , the radial path and the tangential path of  $2\Omega_n$  are the same.

**2.4. Time of Perception of the Observer**

For  $o_0$ , a succession of spinbacks of  $\Omega_{n+1}$  in  $2\Omega_{n+1}=\Omega_n$  can be a discrete movement of fission and fusion of the particle  $\Omega_n$ . If the smallest time of the perception of  $o_0$  is the time of this spinback,  $o_0$  doesn't perceive this periodical fission.  
 For the virtual observer  $o_{-1}$ , the smallest time of one no perceivable spinback of  $\Omega_n$  in  $2\Omega_n$  is the time of the perceivable tangential spinback of  $2\Omega_n$  on  $\Omega_0$ .  
 For  $o_0$ , this time correspond to  $2^{n+1}$  radial spinbacks of  $\Omega_n$  in  $2\Omega_n$  (fig. 5).



**Figure 5 :** dilation of spaces by anticipatory spinbacks in the radial direction.

In the same time,  $\Omega_0$  make the rotation  $\pi/2$  in  $-i\Omega_1$  which becomes  $(i) \times -i\Omega_1 = \Omega_1 \perp i\Omega_1$ . This rotation gives to  $o_{-1}$  in  $\Omega_1=2\Omega_0$  the perception of an anticipatory radial spinback of  $\Omega_n$  in  $2\Omega_n$ .  
 All the embedded anticipatory radial spinbacks (from  $\Omega_n$  to  $\Omega_0$ ) correspond for  $o_0$  to the dilation of the initial space. In fact, this anticipation seems to transform  $\Omega_0$  in  $2\Omega_0$  during the observers' exchanges. When  $o_0$  comes back into  $\Omega_0$  after these exchanges,  $\Omega_0$  has became  $-\Omega_0$  by one spinback in  $\Omega_1$ .  
 For  $o_0$ , the anticipation outside of  $\Omega_0$  has become a past inside of  $-\Omega_0$ . One virtual spinback of  $\Omega_0$  in  $2\Omega_0$  gives one dilation ( $\times 2$ ) of the space  $\Omega_0$  which becomes the dilated space  $(i) \times -i\Omega_1 = \Omega_1 = 2\Omega_0$  for  $o_0$ .

Yet, for  $o_1$ , the first rotation  $\pi/2$  of  $\Omega_0$  in  $\Omega_1$  transforms  $\Omega_0$  in  $i\Omega_0$  and the second ends the spinback which transforms  $i\Omega_0$  in  $i^2\Omega_0 = -\Omega_0$ .

In the same way :  $\pi/2$  of  $\Omega_1$  in  $\Omega_0$  gives the dilated space  $i\Omega_0 = 2\Omega_1$ ,

and :  $\pi/2$  of  $i\Omega_1 = 2\Omega_2$  in  $i\Omega_1$  gives the dilated space  $i^2\Omega_0 = 2i\Omega_1 = 2^2\Omega_2$ .

Thus a succession of dilation ( $\times 2^n$ ) can transform  $\Omega_n$  in the dilated space  $2^n\Omega_n = i^n\Omega_0$ .

If  $n$  is even, the dilated space is  $\pm\Omega_0$ , the doubling is finished. The same observers  $o_0$  and  $o_n$  can make the same transformation in their respective space in different times. So, it is possible to exchange  $o_0$  and  $o_n$  if it is possible to juxtapose  $\Omega_0$  and  $i^n\Omega_0$ . With this difference of transformation's time and with the anticipatory spinback, these observers can exchange their space and time of transformation before the end of the spinback of the space  $\Omega_0$  of  $o_0$ . The first radial spinback of  $\Omega_n$  in  $-\Omega_0$  (fig. 5) is the last radial spinback in  $\Omega_0$  and  $2^{n+2}$  radial spinbacks are necessary to transform  $\Omega_0$  into  $-\Omega_0$ .

Therefore, the rate of spinbacks' speed between  $\Omega_n$  and  $\Omega_0$  is  $2^{n+2}$ .

One minima value of  $n$  determines together the necessary dilation of the space and the difference of perception's time between the observers  $o_0$  and  $o_n$ .

### 2.5. Exchange Condition ( $n=3$ ) and Dilation Condition ( $2^n=8$ )

The initial fission of the particle  $\Omega_n$  in  $\Omega_0$  is also the initial fission of  $\Omega_{n+1}$  in  $\Omega_1$ , of  $\Omega_{n+2}$  in  $\Omega_2, \dots$ , of  $\Omega_{2n}$  in  $\Omega_n$  and so on (fig. 6). When  $\varphi_0 = \varphi_1/2 = \pi/2$ , the space  $\Omega_1$  becomes  $i\Omega_1 \perp \Omega_1$  and because of the operator  $i$ , the perceivable space for  $o_1$  is the dilated space  $i\Omega_0 = 2\Omega_1$ . The particle  $\Omega_{n+1}$  fuses at the centre  $O_0$ .

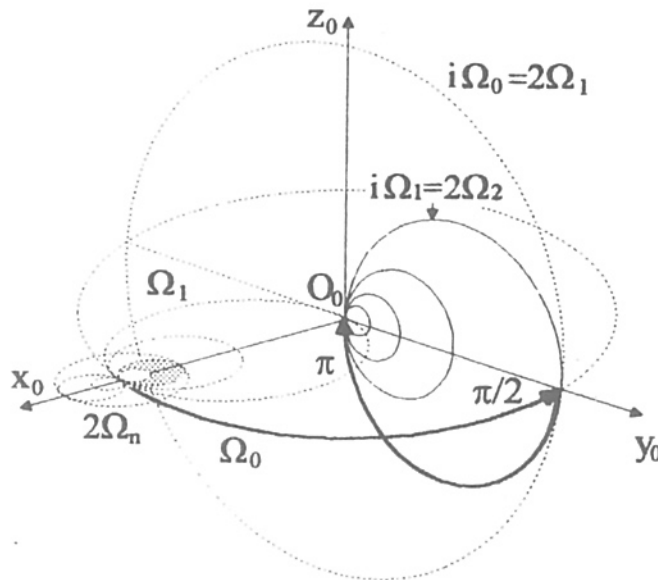


Figure 6 : initial tangential fission of  $\Omega_n$  on  $\Omega_0$  and first radial fusion of  $\Omega_{n+1}$  on  $i\Omega_1$ .

This radial and intermediate fusion gives to  $o_1$  the initial conditions in this dilated space  $i\Omega_0 = 2\Omega_1$  for the perceivable particle  $i\Omega_{n+1} = 2\Omega_n$ . As the spinback of  $i\Omega_1$  in  $i\Omega_0$  is twice faster than the spinback of  $\Omega_1$  in  $\Omega_0$ , the rotation  $\pi/2$  of  $i\Omega_n$  on  $i\Omega_0$  corresponds to the rotation  $\pi/4$  of  $\Omega_n$  on  $\Omega_0$  (fig. 7). It corresponds also to a radial fission of  $i\Omega_n$  on  $i\Omega_0$  and

a tangential fusion of  $i\Omega_{n+1}$  on  $i^2\Omega_0$ . This second intermediate fusion gives to  $o_2$  the initial conditions in this dilated space  $i^2\Omega_0=2^2\Omega_2$  for the perceivable particle  $i^2\Omega_{n+2}=2^2\Omega_n$ . If the initial space  $\Omega_0$  is three dimensional for  $o_0$ , the initial space  $\Omega_0$  and the dilated space  $2^n\Omega_n=i^n\Omega_0$  can be juxtaposing when  $n=3$ . In fact, the rotation  $\pi/2$  of  $i^2\Omega_n$  on  $i^2\Omega_0$  corresponds to  $\pi/4$  of  $i\Omega_n$  on  $i\Omega_0$  and  $\pi/8$  of  $\Omega_n$  on  $\Omega_0$  (fig. 7). It corresponds also to the tangential fission of  $i^2\Omega_n$  on  $i^2\Omega_0$  and the radial fusion of  $i^3\Omega_n$  on  $i^3\Omega_0=8\Omega_3$ .

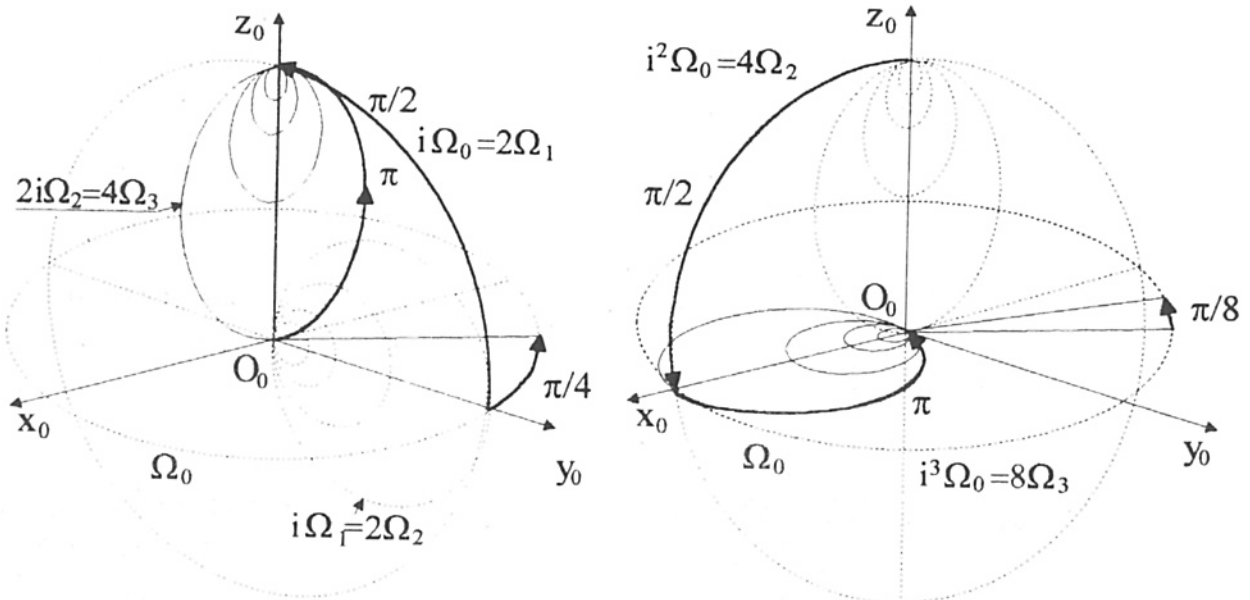


Figure 7 : fission-fusion in  $i\Omega_0=2\Omega_1$  and fission-fusion in  $i^3\Omega_0=2^3\Omega_3$ .

If the initial particle is  $\Omega_3$  on  $\Omega_0$  into  $2\Omega_3$  ( $n=3$ ), the dilated space  $i^3\Omega_0=8\Omega_3$  and  $\Omega_0$  are juxtaposed after the rotation  $\pi/2+\pi/4+\pi/8=7\pi/8=\pi-\pi/8$  of  $2\Omega_3$  on  $\Omega_0$ .

The rotation  $\varphi_3$  of the particle on  $8\Omega_3$  is 8 times faster than the rotation  $\varphi_0$  of the particle on  $\Omega_0$ . The spinback in  $8\Omega_3$  corresponds to the rotation  $\pi/8$  on  $\Omega_0$ .

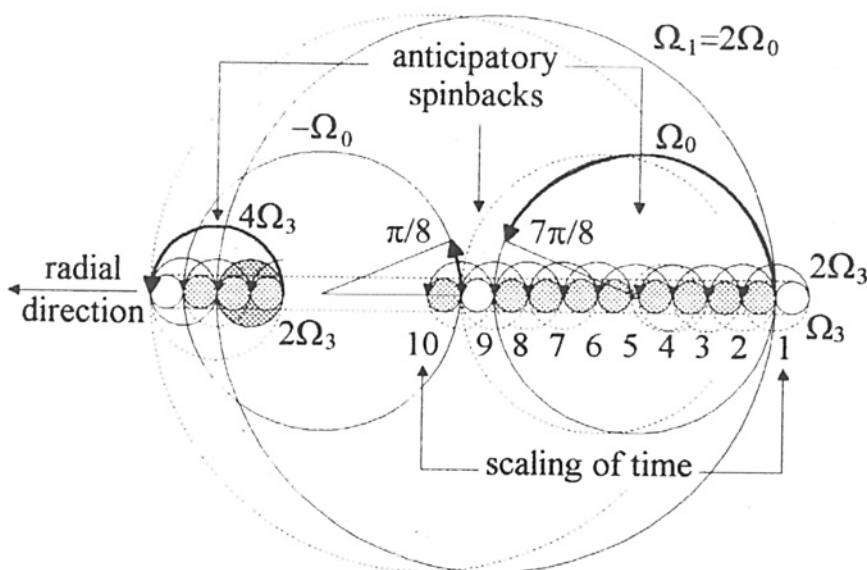


Figure 8 : scaling of time for the exchange of  $o_0$  and  $o_3$



The juxtaposition of the spaces  $\Omega_0$  and  $8\Omega_3$  (after the dilation of  $\Omega_3$  which becomes  $8\Omega_3=\Omega_0$ , after the rotation  $7\pi/8$  on  $\Omega_0$  and after the time of  $1+2+4=7$  radial spinbacks of  $\Omega_3$ ), allows  $o_0$  and  $o_3$  to exchange their spaces (fig. 5&8).

With the dilation of  $\Omega_3$ , the 8<sup>th</sup> and last radial spinback of  $\Omega_3$  into  $\Omega_0$  seems to be the tangential spinback on  $\Omega_0$  for  $o_0$ . It allows  $o_0$  and  $o_3$  to begin their exchange.

## 2.6. The Double Exchange of the Observers in a Ten-Dimensional Space

The third intermediate fusion in  $i^3\Omega_0$  is radial at the centre  $O_0$  of the initial space (fig. 7) which is also the centre  $O_3$  of the dilated space  $i^3\Omega_0$  (fig. 9). The time of the juxtaposition of the spaces  $i^3\Omega_0$  and  $\Omega_0$  allows the exchange of the observers  $o_0$  and  $o_3$ . It is the time of one spinback on  $i^3\Omega_0$  and the time of the rotation  $\pi/8$  on  $\Omega_0$ . For  $o_0$ , the spinback in  $i^3\Omega_0$  is 8 times faster than the spinback in  $\Omega_0$ . During the rotation  $7\pi/8$  on  $i^3\Omega_3$ ,  $o_0$  makes the same transformation again. At the end, the 6<sup>th</sup> fusion in  $i^6\Omega_0$  is tangential (fig. 9).

$i^6\Omega_0$  and  $\Omega_0$  are juxtaposed. For  $o_0$ ,  $i^6\Omega_0=-\Omega_0$  and the initial space  $\Omega_0$  is dilated and the virtual observer  $o_{.1}$  is the real observer  $o_6$ .

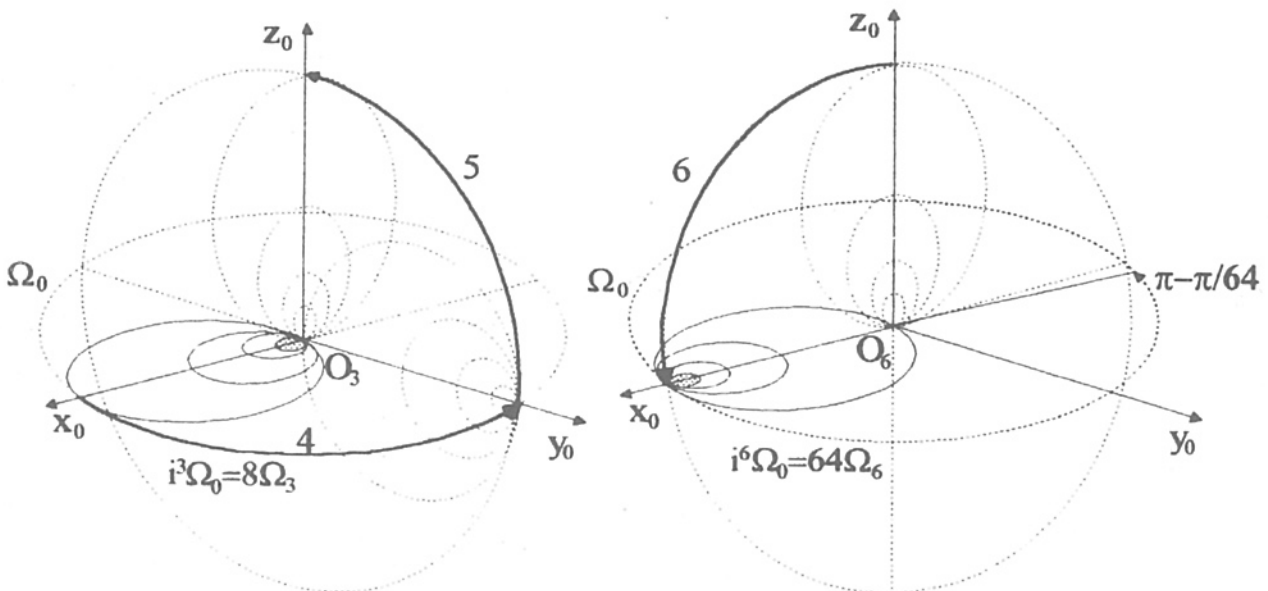
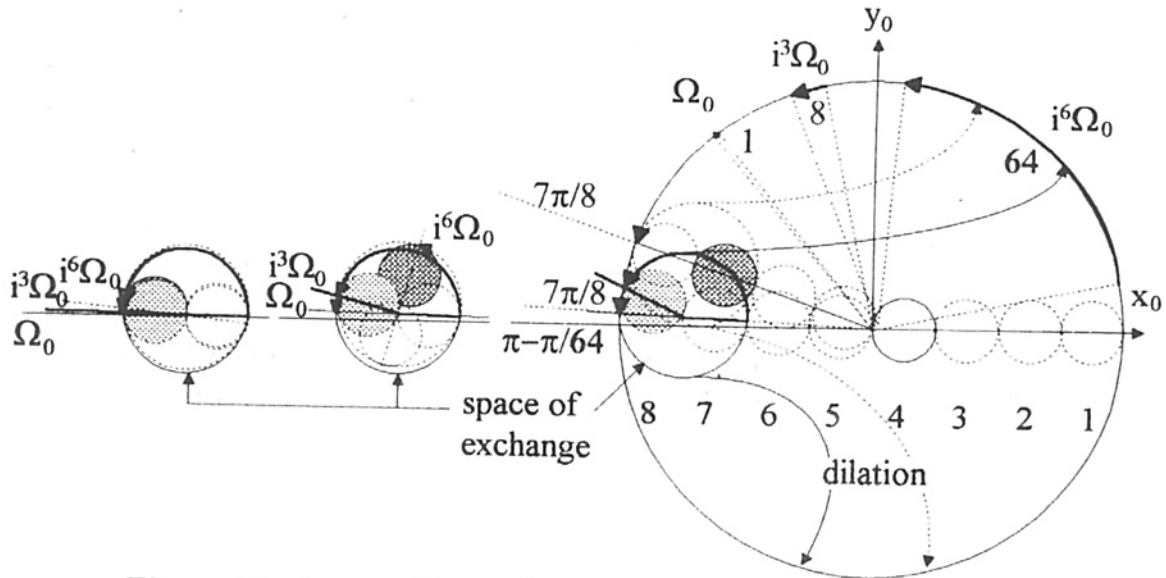


Figure 9 : the sixth fusion on  $i^6\Omega_0=2^6\Omega_6=-\Omega_0$

The transformation of doubling is observed by  $o_0$  in the same way in  $\Omega_0$  and  $-\Omega_0$  but ten times faster in  $\Omega_0$  than in  $-\Omega_0$  (fig. 8). During the tangential rotation  $7\pi/8$  of the particle  $i^6\Omega_3$  on  $i^6\Omega_0$ , the initial particle  $2\Omega_3$  makes the rotation  $\pi/16+\pi/32+\pi/64=\pi-\pi/64$  on  $\Omega_0$  (fig. 10).

So, the spinback of  $2\Omega_3$  on  $\Omega_0$  is not finished. During the last rotation  $\pi/64$ ,  $o_0$  can do the same transformation again, faster and faster. Yet,  $o_0$  must stop the transformation after the sixth transformation. In fact, the first observers' exchange puts  $o_3$  in the initial space :  $o_3$  has not the perception time in  $\Omega_0$ . This observer cannot modify the initial space. In the time of the seventh radial transformation into  $i^6\Omega_0$ , the 8th radial path into

$\Omega_0$  allows  $o_3$  to perceive  $\Omega_0$  (which is becoming  $-\Omega_0$ ). Because of this perception,  $o_3$  can modify the initial space. I can say that the initial space  $\Omega_0$  of  $o_0$  is opening towards  $-\Omega_0$  after the rotation  $7\pi/8$  of the particle  $2\Omega_6$  in the space  $i^6\Omega_0$ . In order to be always the initial observer of  $\Omega_0$  and  $-\Omega_0$ ,  $o_0$  must stop the doubling transformation before this perception.



**Figure 10 :** juxtapositions of spaces for the observers' exchanges

So, there are six doubling transformation to transform the virtual observers  $o_{.1}$  to the real  $o_6$ . And before the end of the spinback in the sixth space  $\Omega_6$ , a final and second exchange puts the observers again in their respective space.

The future of  $o_3$  experimented by  $o_0$  (with  $o_6$ ) in a time no perceivable by  $o_3$  is now the past of  $o_3$ . In other words,  $o_0$  owns an experiment of  $o_3$  in an instantaneous time. For  $o_0$ , it is a time of reflex. Only  $o_0$  has time to experiment with  $o_6$  a new present of  $o_3$  (which is a consequence of the future of  $o_2$ ,  $o_1$  and so  $o_0$ ) and to transform it into a past for  $o_1$ ,  $o_2, \dots, o_6 = o_{.1}$  in a reflex time of  $o_0$  which becomes  $-o_0$  in the initial space  $\Omega_0$  which becomes  $-\Omega_0$ . With this new past (and during the next transformation of  $o_0$ )  $o_3$  can experiment a new future which becomes a past for  $o_6$  and so on. The second spinback of the initial space allows  $-o_0$  to become  $o_0$  again in  $-\Omega_0$  which becomes  $\Omega_0$  again after a new experience. Another exchange during the final juxtaposition of spaces allows  $o_0$  to discover the future which  $o_3$  can do. This future which  $o_0$  experiments with  $o_6$ , give to  $o_0$  a new reflex. So, this discrete transformation which is made in a reflex time of the initial observer, transforms an initial system into anticipatory embedded systems always ready to evolve with the full knowledge of its possibilities.

## 2.7. The Three Perceptions of the Space for the Initial Observer

This doubling transformation uses 4 three-dimensional spaces. But the necessary final juxtaposition uses the initial plane (2 dimensions). So, the space of the doubling

transformation is a ten-dimensional space for the initial observer, but each embedded observer only perceives 3 dimensions. This reduction of dimensions gives to each observer the possibility to be the initial observer of its space during the doubling transformation. Yet, at the end, 9 of the 12 dimensions are juxtaposed and the ten-dimensional space becomes a three-dimensional space for all the embedded observers. The initial observer discovers in the same three-dimensional space the spaces of embedded observers in the time of the final juxtaposition. With scalings of spaces and times, all these observers have the same perception which is the perceptions of a three-dimensional space. Because of these scalings, each observer has different limits of times' and spaces' perception but, at the end of the doubling, three observers of the doubling transformation must perceive the same constant speed of light in three juxtaposed spaces. For that, scalings must disappear. Consequently, for the embedded observers  $o_0$ ,  $o_3$  and  $o_6=o_{-1}$  the perception of the surrounding spaces changes without change of time of transformation.

If  $C_0$  is the constant speed of the doubling transformation for  $o_0$ , I notice  $(C_0)_{o_0}=C_0$  observed by  $o_0$  and I can write the next relations :

$$(C_{-1})_{o_{-1}}=(C_0)_{o_0}=(C_3)_{o_3} \quad (1)$$

$$(C_{-1})_{o_{-1}} \neq (C_0)_{o_{-1}} \neq (C_3)_{o_1} \text{ or : } (C_{-1})_{o_0} \neq (C_0)_{o_0} \neq (C_3)_{o_0} \text{ or : } (C_{-1})_{o_3} \neq (C_0)_{o_3} \neq (C_3)_{o_3} \quad (2)$$

So, I calculated these three speeds of doubling which are never observed by any observer in the same time in the same space. Yet, to begin the doubling transformation ,these three speeds are necessary for the initial observer.

### 3. Three Perceptions of the Speed of Light in the 10-Dimensional Space

#### 3.1. Equation of the Exchange of the Observer and the Speed of Light

With the scaling of times  $e_t$  and the scaling of space between  $o_{-1}$  and  $o_0$  defined in a previous paper (Garnier-Malet, 1997) so that :

$$e_t = 2\sqrt{\pi} \text{ and } e_t e_d = 1 \quad (3)$$

the exchange equation between  $o_{-1}$  and  $o_0$  is :

$$(4\pi R_{-1} R_0)_{o_{-1}} = i(\pi R_0^2)_{o_0} \quad (4)$$

The index  $o_{-1}$  or  $o_0$  signifies : observed by  $o_{-1}$  or  $o_0$ .  $i$  is the operator of the doubling transformation defined in this paper (2.2.).  $R_{-1}$  is the unitary radius so that :

$$(R_{-1})_{o_{-1}} = (1)_{o_{-1}} \quad (5)$$

With the exchange equation (4), I have calculated in the same paper (Garnier-Malet, 1997) the speed of the exchange which defines the perception of the observer :

$$(C_3)_{O_3} = 54.10^6 \pi^2 \sqrt{\pi} (R_3)_{O_3} \text{ in the time of one spinback } (\pi)_{O_3} \quad (6)$$

This speed is constant for the third observer in the third space and with the perception of this embedded space. By definition of the fundamental movement, this perception is independent of the movement of the observer. So, the speed of the exchange is independent of the speed of the observer. Above all, it is the speed of the transformation which is necessary to make the final juxtaposition without any perceivable change of the space. The application of the fundamental movement to the solar system (Garnier Malet, 1997) shows us that the human observer is  $o_3$  in the third space of the Earth. With time  $(\pi)_{O_3}$  and space  $(R_3)_{O_3}$  defined by our planet, I have found :

$$(C_3)_{O_3} = 299\,792 \text{ km/s} \quad (7)$$

### 3.2. The three Perceptions of the Speed of Light.

The definitions of the fundamental movement allows to calculate the three different speeds. These speeds are never observed by the same observer in the same time and space during the doubling transformation but they can explain many paradoxical phenomenon in our Universe.

Each intermediate juxtaposition implies a difference of perception of the doubling movement. This movement of spinbacks is ten times faster in the initial space  $\Omega_0$  than in the doubling space  $i^6\Omega_0 = -\Omega_0$  (fig. 8). The six necessary intermediate juxtapositions (fig. 6-7-9) imply a difference of perception  $10^6$  times faster in the initial space than in the 6<sup>th</sup> space.

The external observer  $o_6 = o_{.1}$  perceives a space 7 times larger than the space of the internal observer  $o_3$ . Because of scalings of spaces and times, in a space 6 times smaller,  $o_3$  perceives the outside 7 times less large than the same space which is perceived by the external observer. During the final juxtaposition, the dilation by 2 of the space and a difference of perception (10 spinbacks for 1) balance the perceptions of the internal and external observers on the common boundary. So, I obtain the following relations :

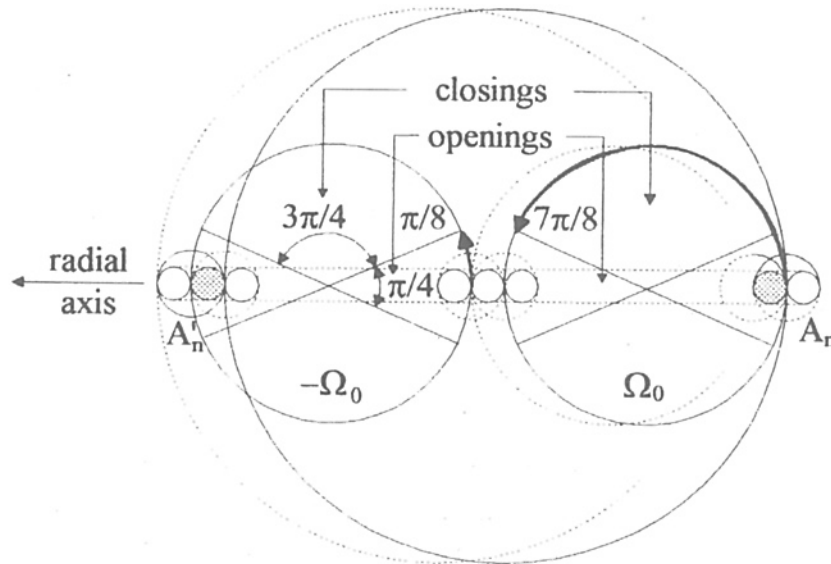
$$(C_{.1})_{O_3} = 7(C_0)_{O_3} = 7(49/12)10^5(C_3)_{O_3} \quad (8)$$

### 3.3. Times of Openings and Closings of Spaces

The radial path of the particle  $\Omega_n$  into  $\Omega_0$  during the tangential path of  $2\Omega_n$  on  $\Omega_0$  is  $\pi R_0$  for all observers (2.3. fig. 4). It is not perceivable by  $o_{.1}$  which only perceives  $2\Omega_n$ . Each radial path is never rectilinear. It is always a tangential path for another observer.

The periodic fissions and fusions of the particle  $\Omega_n$  take place  $\forall n$  on the radial axis  $A_n A'_n$  (fig. 11). These points  $A_n$  and  $A'_n$  are obligatory points of passage when the particles fuse at the end of the spinback.

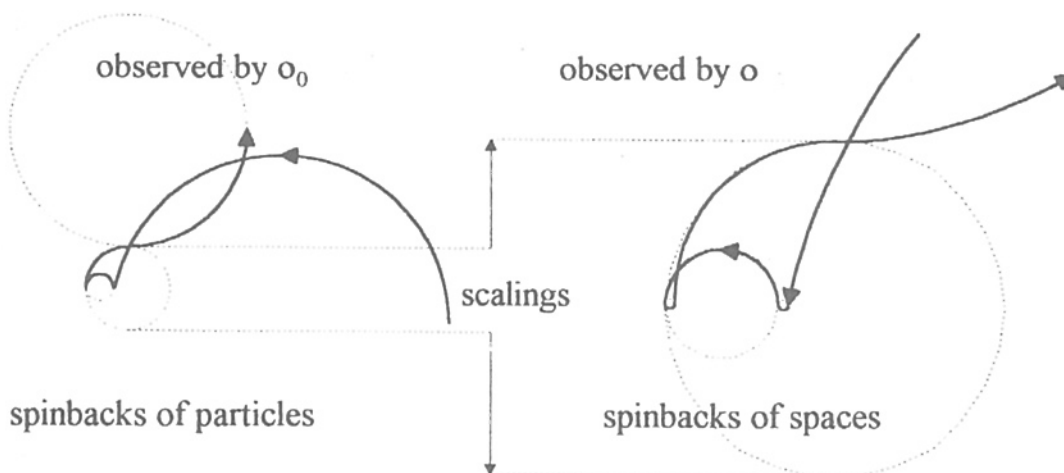
During the spinback, the space is closed. After the rotation  $7\pi/8$ , I can say that the spinback opens and closes the spaces by the junction between the radial and the tangential paths.



**Figure 11 : openings and closings of spaces**

These openings and closings of spaces are a new important discovery.

When the anticipatory embedded spaces are opened during the final juxtaposition, the three speeds of doubling transformation (8) give to the particles the possibility to change its speed (fig. 12).



**Figure 12 : for  $o_0$ , apparent brutal changes of speed and direction**

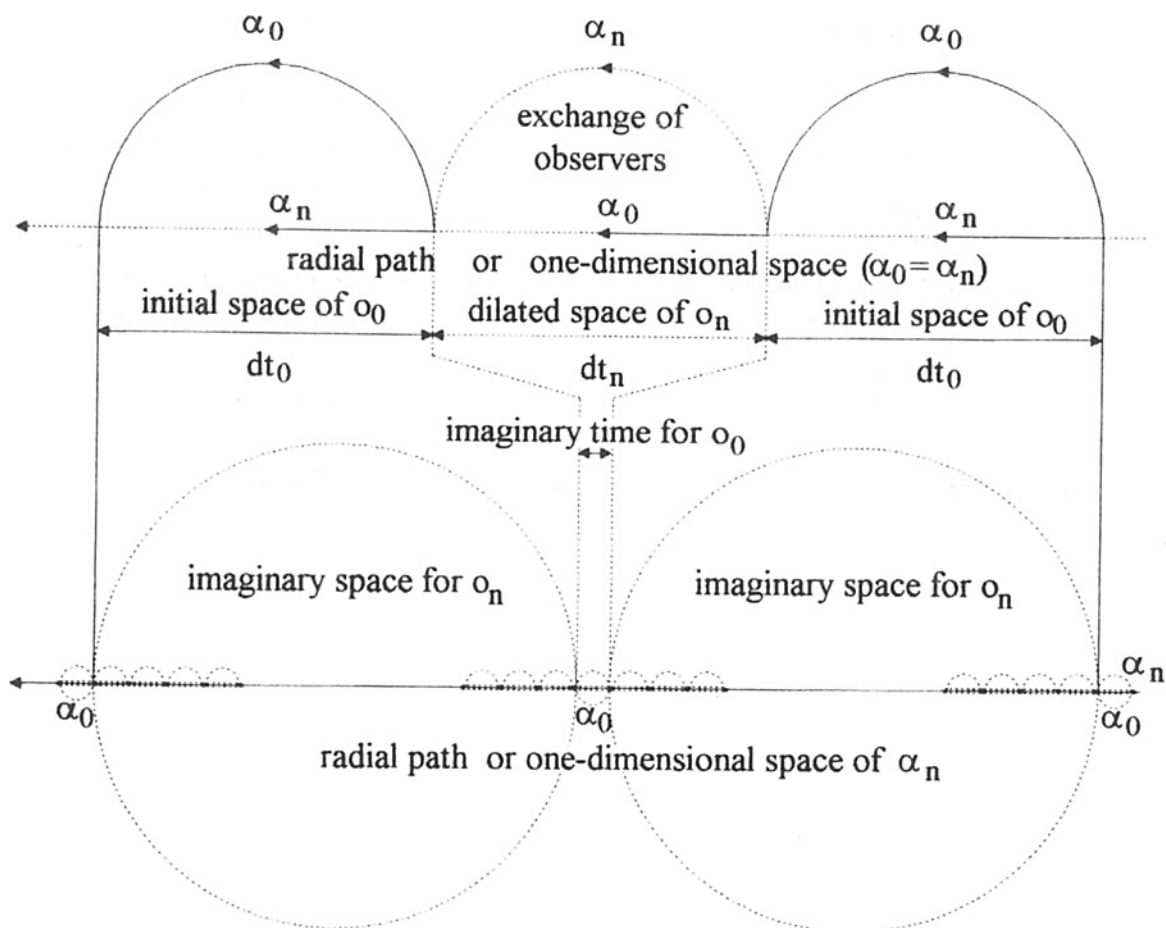
The exchange of the radial and the tangential paths allows a particle (or a space) to change its speed of doubling transformation.

Because of times' and spaces' scalings, the observer sees an abrupt change of speed or direction of the observed particle which makes many spinbacks. When leaving a space, the observer finds a new space in which the speed of light is always the same.

Moreover, the traveller who explores a new space, is moving with the speed of this space which is a particle of another space and so on. He must know the calendar of openings and closings of embedded spaces. In the solar system, this openings can explain the brutal accelerations of the solar particles which are often observed but never explained. In fact, the gravitational balance is never an instantaneous phenomenon but a succession of balances. The openings of spaces can exchange (and never modify) a radial one-dimensional path into a tangential two-dimensional space.

### 3.4. One-Dimensional Space

For the initial observer  $o_0$ , the radial path of  $\alpha_n$  is always one-dimensional. Yet, because of the final exchange of  $o_0$  and  $o_n$ , the intermediate dilated space (fig. 14) and the initial space seems to be identical for  $o_0$  and  $o_n$ .



**Figure 13 :** imaginary three-dimensional space around a one-dimensional space.

For  $\alpha_0$ , the time  $dt_n$  is an imaginary time in the initial space (that is to say a reflex time). For  $\alpha_n$ , the time  $dt_0$  is the spinback time of an imaginary space which becomes perceivable for this observer only at the end of the spinback of the initial space. Yet, for  $\alpha_n$ , this imaginary space is perceivable during the exchange of  $\alpha_n$  and  $\alpha_{2n}$  that is to say in a reflex time. So, the final exchange of  $\alpha_n$  and  $\alpha_0$  transforms a time of dreams into a time of the perception of a imaginary space. For  $\alpha_n$ , it transforms an imaginary space into the initial space. For  $\alpha_0$ , it transforms an imaginary time into the initial time.

### 3.5. Two-Dimensional Space

The initial observer  $\alpha_0$  observes in the initial plane space  $\Omega_0$  the initial particle  $\alpha_0$  which makes its tangential spinback (fig. 15). When  $\varphi_0 = \pi/4, \pi/2, 3\pi/4, \pi-\pi/64, \pi$ , the tangential positions of  $\alpha_0$  on  $\Omega_0$  (1-2-3-4-5-5) correspond to internal or radial fusions of the particle (positions 1-2-4-5-6).

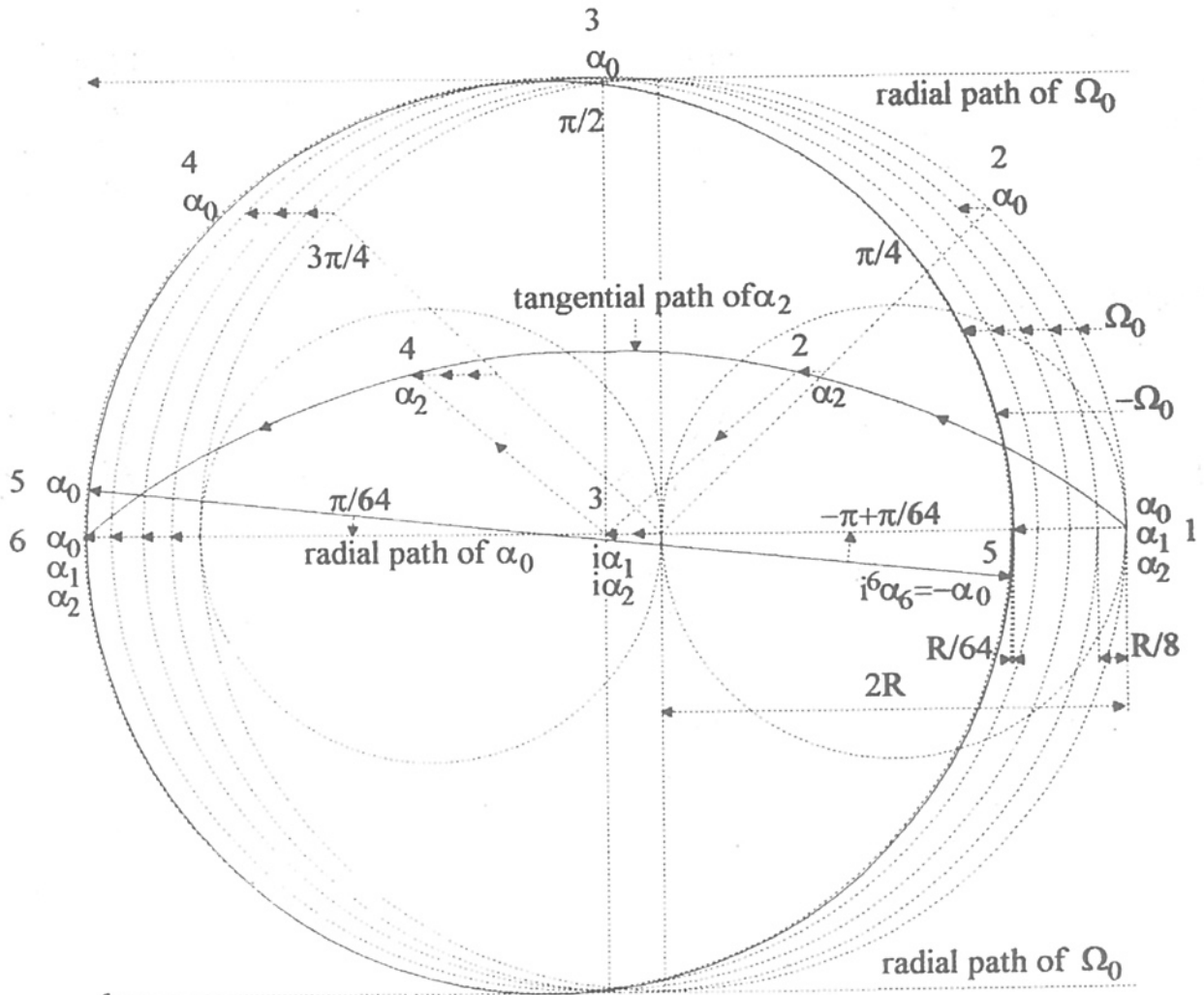


Fig. 14 : doubling in the initial two-dimensional space of the initial observer.

When  $\varphi_0 = \pi - \pi/64$ , the tangential position of  $\alpha_0$  on  $\Omega_0$  (position 5) corresponds to a radial position of  $i^6 \alpha_6$  on a dilated space  $i^6 \Omega_6$  (position 5) which seems to be  $-\Omega_0$  for  $\alpha_0$

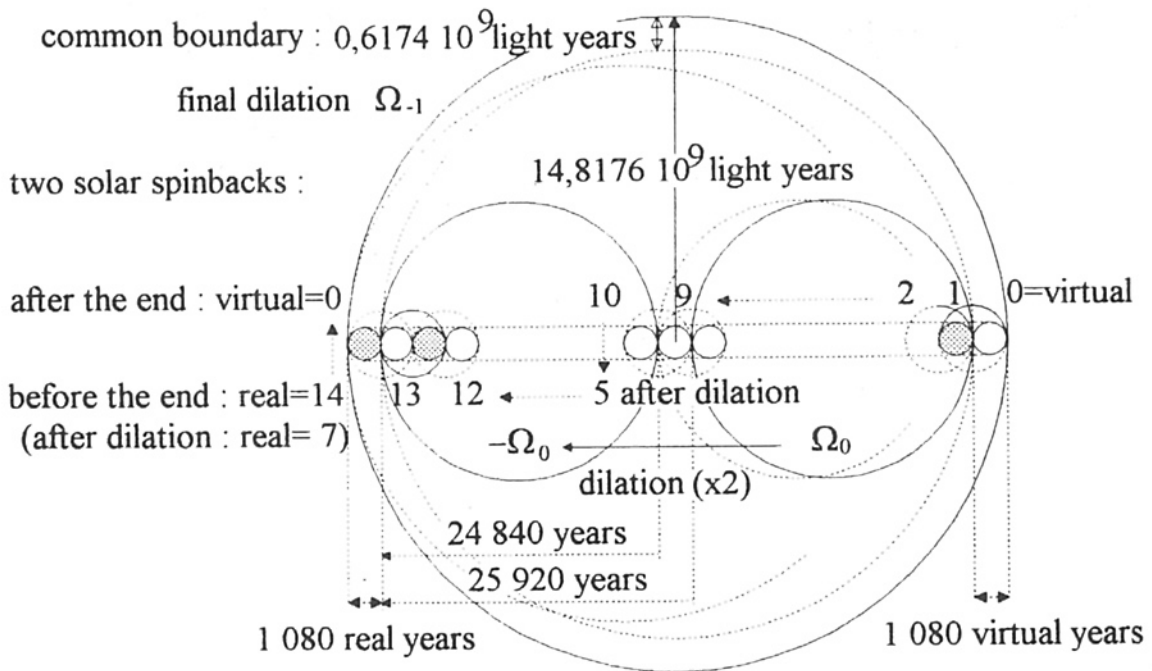
after the rotation  $-\varphi_0 = -\pi + \pi/64$  ( $n^{\circ}2.6$ ). For  $o_0$ , the doubling of the particle  $\alpha_0$  exists on  $-\Omega_0$  which is the position of  $\Omega_0$  before the 64<sup>th</sup> rotation  $\pi/64$  of  $\alpha_0$  on  $\Omega_0$  and before the 64<sup>th</sup> spinback of  $-\alpha_0$  on  $-\Omega_0$  (64 times faster than the spinback of  $\alpha_0$  on  $\Omega_0$ ).

The dilation of the radial space  $-\Omega_0$  allows the observers' exchange just before this last 64<sup>th</sup> spinback. For  $o_0$  which doesn't perceive  $\alpha_2$  in  $\Omega_0$ , the fusions of  $\alpha_2$  are perceivable in the dilated plane space  $-\Omega_0$  where they seem to be on a tangential path (positions : 1,2,4,6) around the radial path of  $\alpha_0$  (positions 1&6).

Because of the dilation of the radial space  $i^6\Omega_6 = -\Omega_0$ , the particle  $\alpha_2$  seems to be a perceivable tangential particle  $-\alpha_{.1} = i^6\alpha_2$  for  $o_0$ . Only a final dilation (which corresponds to the 64<sup>th</sup> spinback of  $-\alpha_0$  on  $-\Omega_0$  at the end of the spinback of  $\Omega_0$  into  $\Omega_{.1}$ ) allows  $\Omega_0$  and  $-\Omega_0$  to juxtapose in the initial plane which becomes the new initial doubled plane space  $\pm\Omega_0$  in a new virtual plane space or horizon  $\Omega_{.1}$ .

### 3.6. Final Dilation of Our Perceivable Three-Dimensional Universe

The three different perceptions of the speed of light allow the observer  $o_3$  (who we are) to calculate the dimensions of our perceivable Universe at the end of the solar cycle (24840 years) without forgotten the anticipation (1080 years) before and after this cycle (fig. 13). Now, after a final dilation (or expansion), our Universe becomes the initial dilated space of  $o_{.1}$  which corresponds to the final dilation of the initial solar space for  $o_3$ . It is the goal of the doubling which must allow the observers  $o_0$  and  $o_3$  to exchange spaces and times of transformation without modifying their initial space during their time of perception.



**Fig. 15** : the expansion of our Universe at the end of the solar spinback



The first tangential spinback of  $\Omega_0$  dilates the space ( $\times 2$ ). So, the 10<sup>th</sup> radial spinbacks into  $\Omega_0$  becomes the 5<sup>th</sup> into  $-\Omega_0$ . The 14<sup>th</sup> radial spinback into  $-\Omega_0$  ends the second tangential spinback of  $\Omega_0$  (or the first of  $-\Omega_0$ ). After the dilation of the second spinback of  $\Omega_0$ , the 14<sup>th</sup> becomes the 7<sup>th</sup> into  $-(-\Omega_0)$  which becomes a new space  $\Omega_0$  into  $-\Omega_1$ . This last real radial spinback into  $-\Omega_0$  of  $\Omega_1$  becomes a virtual spinback outside of this new space for the initial observer  $o_{-1}$  which becomes  $o_0$  again in  $-\Omega_1$ .

The equation (8) give the rate  $(343/12)10^5$  of perception of the doubling speed between  $o_{-1}$  and  $o_3$ . Because the dilation ( $\times 2$ ) and the acceleration of the movement (from 1 to 10) between the spaces  $\Omega_0$  and  $-\Omega_0$ , the radius of the circular horizon of  $o_3$  corresponds to the years which are necessary for the radial path when the speed of the doubling is no more  $(C_3)_{o_3}$  but  $(C_{-1})_{o_3}=(343/12)10^5(C_3)_{o_3}$ .

Therefore, for the observer  $o_3$ , this distance becomes the following light years :

$$(R_{\text{Universe}})_{o_3}=25\,920 \times (2/10) \times (343/12)10^5=14,8176\,10^9 \text{ light years} \quad (9)$$

So, at the end of the solar spinback, it is the maximum dilation of our Universe which is perceivable by the observer  $o_3$  (who we are).

The anticipation (fig. 13) corresponds to a common boundary (or a perceivable space corresponding to 1 080 years) between the spaces of  $o_{-1}$  and  $o_3$  :

$$1\,080 \times (2/10) \times (343/12)10^5=0,6174\,10^9 \text{ light year} \quad (10)$$

We must notice that the age of the Universe cannot be calculated by using the speed of light  $(C_3)_{o_3}=299\,792$  km/s. Only the number of the spinbacks of our Universe can give to us this age. It is not possible to observe this number before the end of our solar spinback. Only the beginning of the next spinback allows  $o_3$  to perceive the real radial distance into the Universe which corresponds to the real age of the Universe. Yet, with the knowing of the age of our solar system  $\Delta t_s$ , it is possible to calculate this number. Inside of the solar system, we can observe the radial path of the Universe which corresponds to the following light years :

$$14,818\,10^9=\text{equation (9)}$$

$$\text{minus the final space of anticipation } 0,617\,10^9=\text{equation (10)}$$

$$\text{minus the virtual initial space } 0,617\,10^9=\text{equation (10)}.$$

So this radial path is for  $o_3$  :

$$14,818\,10^9-0,617\,10^9-0,617\,10^9=13,583\,10^9 \text{ light years} \quad (11)$$

By several observations and experiments, we know that our solar system is about  $4,5\,10^9$  years old. Therefore,  $13,583\,10^9/(4,5\,10^9)=3,018$  spinbacks of the Universe are been necessary.

We are now at the end of the solar spinback (24 840 years) which must correspond to the end of one spinback of the Universe. Consequently, this spinback must be strictly the third spinback and the age of our solar system must be exactly :

$$\Delta t_{\text{solar}} = 13,583 \cdot 10^9 / 3 = 4,528 \cdot 10^9 \text{ years} \quad (12)$$

So, I verify the link (equations : 3,4,5) between the dilation (or expansion) of our Universe (space of  $o_0$ ) and the age of our solar system (time of  $o_3$ ).

It is very important to notice that our perceivable Universe (observed by Hubble's telescope) is going to correspond to the theoretic perceivable distance  $14,8176 \cdot 10^9$  light years (9). So, this final expansion of our Universe opens all the embedded spaces just at the end of the cycle of our solar space  $-\Omega_0$  in the Universe  $\Omega_{-1}$  which is actually becoming  $\Omega_0$  in  $-\Omega_{-1}$ . After 24 840 years of closing, this spaces opening involves observers' exchanges just before this end.

#### 4. Conclusion

The fundamental movement of doubling which transforms any evolution system in anticipatory embedded systems allows us to know the solar cycle of 24 840 years (Garnier-Malet, 1997) and, above all, to understand the many perturbations which the present end of this cycle brings now to our planet.

These perturbations are the consequences of a necessary new solar balance which depends on very important new physical notion : the openings and closings of six double spaces embedded in the same doubling transformation.

These openings which imply times of gravitational modifications, are the principal cause of future perturbations of our space during the final solar juxtaposition which puts three embedded observers  $o_0, o_3, o_6 = o_{-1}$  in the same three dimensional space. They balance together our planetary envelope in our solar system and our planet around its kernel which is a space using the same transformation.

Six successive openings of the spaces modify the perception of our Universe at the end of the solar cycle of doubling transformation. In six times, this very imminent end gives us the possibility to observe our surrounding initial ten-dimensional space, to understand the new planetary perturbations and maybe to avoid them. For that, we must use and anticipate the movements of doubling of all anticipatory embedded spaces, without never forgetting the particles' movements which are always spaces' movements of another observer embedded in the same doubling transformation.

It is impossible to change one particle of any space without modifying the space. It is dangerous to change spaces without reason because that changes the particles of spaces. If we can understand that, we will begin to understand our responsibility in the future planetary perturbations.

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